

Continuous Distributions

| Distribution | pdf | Mean | Variance | R function |
|---------------------------|--|-------------------------------|--|---------------------|
| Beta(α, β) | $\frac{\Gamma(\alpha+\beta)}{\Gamma(\alpha)\Gamma(\beta)}x^{\alpha-1}(1-x)^{\beta-1}; x \in [0, 1]; \alpha > 0, \beta > 0$ | $\frac{\alpha}{\alpha+\beta}$ | $\frac{\alpha\beta}{(\alpha+\beta)^2(\alpha+\beta+1)}$ | <code>rbeta</code> |
| Gamma(α, β) | $\frac{\beta^\alpha}{\Gamma(\alpha)}x^{\alpha-1}e^{-\beta x}; x > 0; \alpha > 0; \beta > 0$ | $\frac{\alpha}{\beta}$ | $\frac{\alpha}{\beta^2}$ | <code>rgamma</code> |
| Exponential(λ) | $\lambda e^{-\lambda x}; x \geq 0; \lambda > 0$ | $\frac{1}{\lambda}$ | $\frac{1}{\lambda^2}$ | <code>rexp</code> |
| Normal(μ, σ^2) | $\frac{1}{\sqrt{2\pi\sigma^2}}e^{-\frac{(x-\mu)^2}{2\sigma^2}}; x \in \mathbb{R}; \mu \in \mathbb{R}; \sigma^2 > 0$ | μ | σ^2 | <code>rnorm</code> |
| Uniform(a, b) | $\frac{1}{b-a}; x \in [a, b]; -\infty < a < b < \infty$ | $\frac{1}{2}(a+b)$ | $\frac{1}{12}(b-a)^2$ | <code>runif</code> |

Discrete Distributions

| Distribution | pmf | Mean | Variance | R function |
|-------------------------|--|-----------------|--------------------|-------------------------------|
| Bernoulli(p) | $p^x(1-p)^{1-x}; x \in \{0, 1\}; p \in [0, 1]$ | p | $p(1-p)$ | <code>rbinom(size = 1)</code> |
| Binomial(n, p) | $\binom{n}{x}p^x(1-p)^{n-x}; x \in \{0, 1, \dots, n\}; p \in [0, 1]$ | np | $np(1-p)$ | <code>rbinom</code> |
| Discrete Uniform(N) | $\frac{1}{N}; x \in \{1, \dots, N\}; N \in \mathbb{N}$ | $\frac{N+1}{2}$ | $\frac{N^2-1}{12}$ | <code>sample</code> |
| Geometric(p) | $(1-p)^{x-1}p; x \in \{1, 2, 3, \dots\}; p \in [0, 1]$ | $\frac{1}{p}$ | $\frac{1-p}{p^2}$ | <code>rgeom</code> |
| Poisson(λ) | $\frac{\lambda^x e^{-\lambda}}{x!}; x \in \{0, 1, 2, \dots\}; \lambda > 0$ | λ | λ | <code>rpois</code> |